# KINETICS OF CATALYZED REACTION OF METHANOL WITH WATER VAPOUR 

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Kinetics of methanol conversion with water vapour on a low-temperature catalyst of the composition $\mathrm{CuO}-\mathrm{ZnO}-\mathrm{Cr}_{2} \mathrm{O}_{3}-\mathrm{Al}_{2} \mathrm{O}_{3}$ was studied at 1 atm , at temperatures $220-250^{\circ} \mathrm{C}$ and at different $\mathrm{CH}_{3} \mathrm{OH}: \mathrm{H}_{2} \mathrm{O}$ ratios. The reaction course can be expressed by a kinetic equation in the form $r=k p_{\mathrm{A}}^{0.4} p_{\mathrm{B}}^{0.6}$, where $p_{\mathrm{A}}$ and $p_{\mathrm{B}}$ are partial pressures of methanol and water vapour, respectively. This relation can be simplified with satisfactory accuracy to the form $r=k\left(p_{\mathrm{A}} \rho_{\mathrm{B}}\right)^{0.5}$. Of the relations, based on the Langmuir-Hinshelwood concepts, the equation $r=k K_{1} K_{2} p_{\mathrm{A}} p_{\mathrm{B}}$ : $:\left(1+K_{1} p_{\mathrm{A}}+K_{2} p_{\mathrm{B}}\right)^{2}$ was found to be suitable which was derived under the assumption that the rate controlling process is the surface reaction $\mathrm{CH}_{3} \mathrm{OHn}+\mathrm{H}_{2} \mathrm{On} \rightarrow 3 \mathrm{H}_{2}(\mathrm{~g})+\mathrm{CO}_{2}(\mathrm{~g})+$ +2 n .

One of the possible ways of preparation of hydrogen for oxygen-hydrogen fuel cells is the catalytic conversion of methanol with water vapour. This procedure has been the subject of several studies ${ }^{1-11}$. Most of these works, however, are concerned with practical problems connected with the application of the conversion reaction and they deal above all with the preparation and application possibilities of suitable catalysts. However, detailed data on the kinetics of this reaction are so far lacking. This question has been dealt with only in papers ${ }^{5,6,9,10}$ in which the composition of the inlet gas and the formation of by-products is studied.

The aim of the present paper was to determine the principal kinetic data of the conversion reaction on a selected low-temperature catalyst which could serve in designing the reaction conditions for the above-mentioned method of the preparation of hydrogen and at the same time could be a basis for the concepts on the course of the reaction itself.

Conversion of methanol by water vapour can be described by the over-all equation

$$
\begin{equation*}
\mathrm{CH}_{3} \mathrm{OH}+\mathrm{H}_{2} \mathrm{O} \rightleftarrows \mathrm{CO}_{2}+3 \mathrm{H}_{2}, \quad \Delta H_{298}^{0}=11.83 \mathrm{kcal} / \mathrm{mol} \tag{A}
\end{equation*}
$$

According to this equation, the outlet gas should contain, at total conversion of methanol after condensation of water vapour, which is always used in excess, $25 \% \mathrm{CO}_{2}$ and $75 \% \mathrm{H}_{2}$. However, the mixture after conversion contains always also carbon monoxide. Thus it is evident that the reaction proceeds via a complex mechanism
and can be, in the first approximation, considered to consist of two consecutive reactions, the first step being the decomposition of methanol to hydrogen and carbon monoxide which in the second step reacts with water vapour

$$
\begin{gather*}
\mathrm{CH}_{3} \mathrm{OH} \rightleftarrows \mathrm{CO}+2 \mathrm{H}_{2}, \Delta H_{298}^{0}=21 \cdot 66 \mathrm{kcal} \mathrm{~mol}^{-1}  \tag{B}\\
\mathrm{CO}+\mathrm{H}_{2} \mathrm{O}  \tag{C}\\
\rightleftarrows \mathrm{CO}_{2}+\mathrm{H}_{2}, \Delta H_{298}^{0}=-9.83 \mathrm{kcal} \mathrm{~mol}^{-1}
\end{gather*}
$$

In addition to these main reactions, several side reactions can of course proceed in this system whose products are methane, higher hydrocarbons, alcohols and formaldehyde ${ }^{9-12}$. The course of these side reactions can be minimalized by a suitably chosen catalyst and by reaction conditions so that the study can then be limited to the analysis of the mentioned two reactions.

These partial reactions, particularly that of carbon monoxide with water vapour, were the subject of a number of studies. Reaction $(B)$ was investigated mainly from the standpoint of methanol synthesis ${ }^{\mathbf{1 2 , 1 5}}$. A review of works on the shift reactions of carbon monoxide with water vapour is given in papers ${ }^{13,14}$. From this survey it is clear that so far no accordance has been attained as to the course of even this most simple reaction; on the contrary, the results of different authors are often contradictory.

Conversion of methanol by water vapour is possible to assume to consist of two steps, according to Eqs $(B)$ and $(C)$. The equilibrium constants of the decomposition of methanol, $K_{2}^{\prime}$, and of conversion of carbon monoxide by water vapour, $K_{3}^{\prime}$, are given by the expressions

$$
\begin{align*}
K_{2}^{\prime} & =\frac{(x-y) \cdot(2 x+y)^{2}}{(1+2 x+a)^{2}(1-x)} \cdot P^{2}  \tag{1}\\
K_{3}^{\prime} & =y(2 x+y) /(x-y)(a-y) \tag{2}
\end{align*}
$$

where $x$ is the conversion of $\mathrm{CH}_{3} \mathrm{OH}$ in mol, $y$ is the conversion of CO in mol, $a$ is the number of mol of water vapour, $P$ is the total pressure. The values of thermodynamic quantities necessary for determining the equilibrium constants and for calculating the equilibrium composition were taken from the literature ${ }^{16}$.

By simultaneous solution of Eqs (1) and (2) we obtained the values of $x$ and $y$ from which the equilibrium composition of the mixture at various temperatures could be calculated, as shown in Table I. From the values presented it is clear that at the given temperatures methanol can almost completely decompose to carbon monoxide and hydrogen. Actually, also this reaction proceeds, for kinetic reasons, only to a certain degree and it is possible to calculate the equilibrium content of CO in the reaction mixture after condensation of the non-reacted water vapour which
corresponds to a certain degree of methanol decomposition. These equilibrium values of CO are presented in Table II.

From the practical point of view it is desirable that the content of $\mathrm{CO}_{2}$ in the gaseous mixture might be as low as possible and the total conversion of $\mathrm{CH}_{3} \mathrm{OH}$ as high as possible. The attainable content of CO is the smaller the lower is the conversion temperature and the lower is the degree of methanol decomposition according to Eq. ( $B$ ). Increase in pressure results in a shift of the equilibrium to the higher degree of decomposition, however, even at 10 atm , the equilibrium is shifted rather to the right and the pressure dependence in this range of pressures is not too much manifested. The equilibrium is also shifted owing to the fact that CO is immediately consumed in reaction $(C)$. The decrease of the CO content can therefore be realized in two ways, either by lowering the temperature or by using excess of water. A great excess of water is of course not advantageous. Lowering of temperature is limited by the activity of the catalyst used.

## EXPERIMENTAL AND RESULTS

Apparatus. The course of the reaction was followed in an isothermal integral reactor, schematically shown in Fig. 1. A solution of methanol and water is continuously fed by a piston micropump

Table I
Dependence of Equilibrium Values of $x$ and $y$ and of Equilibrium Content of CO after Condensation of Water Vapour on Temperature and on Molar Ratio $\mathrm{CH}_{3} \mathrm{OH}: \mathrm{H}_{2} \mathrm{O}$

| $\mathrm{CH}_{3} \mathrm{OH}: \mathrm{H}_{2} \mathrm{O}$ | ${ }^{\circ} \mathrm{C}$ | $x$ | $y$ | CO eq. <br> $\%$ |
| :---: | :---: | :---: | :---: | :---: |
| $1: 1$ | 200 | 0.9988 | 0.8932 | 2.72 |
|  |  | 230 | 0.9995 | 0.8643 |
|  | 250 | 0.9997 | 0.8368 | 4.50 |
| $1: 1.2$ | 300 | 0.9999 | 0.7706 | 6.08 |
|  | 200 | 0.9994 | 0.9503 | 1.24 |
|  | 230 | 0.9998 | 0.9264 | 1.87 |
|  | 250 | 0.9999 | 0.9017 | 2.52 |
|  | 300 | 0.9999 | 0.8380 | 4.22 |
|  | 200 | 0.9998 | 0.9756 | 0.61 |
|  | 230 | 0.9999 | 0.9608 | 1.00 |
|  | 250 | 0.9999 | 0.9439 | 1.42 |
|  | 300 | 1.0000 | 0.8946 | 2.71 |
|  | 200 | 0.9999 | 0.9872 | 0.32 |
|  | 230 | 0.9999 | 0.9788 | 0.53 |
|  | 250 | 1.0000 | 0.9688 | 0.79 |
|  | 300 | 1.0000 | 0.9363 | 1.62 |
|  |  |  |  |  |
|  |  |  |  |  |

Table II
Values of CO Content in Dependence on Methanol Decomposition, Temperature and Molar Ratio $\mathrm{CH}_{3} \mathrm{OH}: \mathrm{H}_{2} \mathrm{O}$ after Condensation of Water Vapour

| $\begin{gathered} \text { Molar ratio } \\ \mathrm{CH}_{3} \mathrm{OH}: \mathrm{H}_{2} \mathrm{O} \end{gathered}$ | $x$ | $\% \mathrm{CO}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $200^{\circ} \mathrm{C}$ | $230^{\circ} \mathrm{C}$ | $250{ }^{\circ} \mathrm{C}$ | $300^{\circ} \mathrm{C}$ |
| 1:1 | 0.9 | 1.66 | $2 \cdot 36$ | 3.05 | 4-70 |
|  | 0.7 | 0.63 | 1.01 | 1.44 | $2 \cdot 68$ |
|  | 0.5 | $0 \cdot 26$ | 0.42 | 0.63 | $1 \cdot 29$ |
|  | $0 \cdot 3$ | 0.09 | $0 \cdot 15$ | 0.22 | 0.48 |
| $1: 1 \cdot 2$ | 0.9 | 0.84 | $1 \cdot 32$ | 1.84 | $3 \cdot 31$ |
|  | 0.7 | 0.40 | $0 \cdot 65$ | 0.96 | 1.90 |
|  | 0.5 | $0 \cdot 18$ | $0 \cdot 31$ | 0.46 | 0.97 |
|  | $0 \cdot 3$ | 0.07 | $0 \cdot 12$ | 0.17 | 0.38 |
| $1: 1 \cdot 5$ | 0.9 | 0.46 | 0.75 | 1.09 | $2 \cdot 16$ |
|  | 0.7 | 0.25 | 0.42 | $0 \cdot 63$ | 1.30 |
|  | 0.5 | $0 \cdot 13$ | 0.22 | 0.33 | 0.70 |
|  | 0.3 | 0.05 | 0.09 | $0 \cdot 13$ | 0.28 |
| 1:2 | 0.9 | $0 \cdot 26$ | 0.43 | 0.64 | $1 \cdot 33$ |
|  | 0.7 | $0 \cdot 16$ | 0.26 | $0 \cdot 40$ | 0.84 |
|  | 0.5 | 0.09 | $0 \cdot 15$ | $0 \cdot 22$ | 0.48 |
|  | $0 \cdot 3$ | 0.04 | 0.06 | $0 \cdot 09$ | 0.20 |



Fig. 1
Scheme of the Apparatus
For description see text.


Fig. 2
Kinetic Isotherms for Molar Ratio $\mathrm{CH}_{3} \mathrm{OH}$ : $: \mathrm{H}_{2} \mathrm{O}$ 1: 1.5

Pressure 1 atm . Temperature: $1250^{\circ} \mathrm{C}$, $2240^{\circ} \mathrm{C}, 3230^{\circ} \mathrm{C}, 4220^{\circ} \mathrm{C} . W / F$ is given in $\mathrm{gh} \mathrm{mol}{ }^{-1}$.

2 from a measuring burette 1 into preheater 3 , heated to $120^{\circ} \mathrm{C}$. Here the solution is evaporated and the gaseous mixture proceeds into reactor 4 , placed in a block oven 5 with controlled heating. Temperature within the reactor was measured by means of a Fe -Constantan thermocouple, placed in the bed of catalyst 6 . The catalyst was coated in the reactor on a support made of sintered glass. The converted gas is led from the reactor into the cooler 7 where the unreacted portions of water and methanol are condensed and caught in the separator 8 . The gas is then led through thermostat 9 into the thermostated flowmeter 10. Constant pressure in the apparatus was maintained by means of manostat 12. Gas samples for analysis were taken before manostat 11. The determination of $\mathrm{CO}_{2}$ was carried out in an Orsat apparatus, CO was determined using gas chromatograph Chrom 3-I (Laboratorní pristroje, Prague). In the place, where methanol is fed in, an inlet is attached, allowing to dose the inert gas or the reaction products into the reaction mixture and also to feed the $\mathrm{H}_{2}-\mathrm{N}_{2}$ mixture for the reduction of the catalyst.

The catalyst used. On the basis of preliminary experiments a low-temperature catalyst of the type $\mathrm{CuO}-\mathrm{ZnO}-\mathrm{Cr}_{2} \mathrm{O}_{3}-\mathrm{Al}_{2} \mathrm{O}_{3}$ was chosen. The catalyst used, prepared in the laboratory,

## Table III

Constants of the Interpolated Polynomials

| $\mathrm{CH}_{3} \mathrm{OH}: \mathrm{H}_{2} \mathrm{O}$ | ${ }^{\circ} \mathrm{C}$ | $\begin{gathered} a_{0} \\ \mathrm{~g} \mathrm{~h} \mathrm{~mol}^{-1} \end{gathered}$ | $\underset{\mathrm{g} \mathrm{~h} \mathrm{~mol}^{-1}}{a_{1}}$ | $\underset{\mathrm{g} \mathrm{~h} \mathrm{~mol}^{-1}}{a_{2}}$ | $\underset{\mathrm{g} \mathrm{M} \mathrm{~mol}^{-1}}{a_{3}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $1: 1$ | 220 | 0.005 | 10.335 | 28.510 |  |
|  | 230 | 0.023 | 7.032 | $10 \cdot 441$ |  |
|  | 240 | 0.043 | 2.702 | 11.502 |  |
|  | 250 | 0.059 | $-1.475$ | 12.649 |  |
| 1:1•1 | 220 | -0.005 | 10.591 | 28.577 |  |
|  | 230 | 0.050 | 5.754 | 13.874 |  |
|  | 240 | 0.021 | 3.239 | $10 \cdot 580$ |  |
|  | 250 | 0.033 | 1.656 | 9.763 |  |
| 1:1.3 | 220 | $-0.009$ | $6 \cdot 414$ | 25.333 |  |
|  | 230 | -0.005 | 3.450 | 19.547 |  |
|  | 240 | 0.017 | 2.861 | 8.797 |  |
|  | 250 | --0.006 | 11.315 | $-25.762$ | $24 \cdot 693$ |
| 1:1.5 | 220 | 0.003 | 2.1512 | 26.428 |  |
|  | 230 | $-0.005$ | --0.327 | 16.972 |  |
|  | 240 | -0.003 | 9.782 | $-21.470$ | $24 \cdot 483$ |
|  | 250 | 0.026 | --4.220 | $13 \cdot 341$ |  |
| 1:2 | 220 | ---0.044 | 3.780 | $21 \cdot 357$ |  |
|  | 230 | 0.017 | --3.103 | $20 \cdot 671$ |  |
|  | 240 | 0.028 | -3.958 | 14.235 |  |
|  | 250 | $-0.002$ | 28.891 | -77.909 | 58.3855. |

had the following composition: $22 \cdot 3 \% \mathrm{CuO}, 17 \cdot 5 \% \mathrm{Al}_{2} \mathrm{O}_{3}, 24 \cdot 2 \% \mathrm{ZnO}$ and $22 \cdot 5 \% \mathrm{Cr}_{2} \mathrm{O}_{3}$. Loss by ignition was $14.5 \%$ bulk weight $0.573 \mathrm{~g} / \mathrm{cm}^{3}$, total surface area of the catalyst in non-reduced state $262 \mathrm{~m}^{2} / \mathrm{g}$. For kinetic studies 4 g of the catalyst were used of the grain size $0.8-1.0 \mathrm{~mm}$. The catalyst was mixed with crushed glass of the same grain size in the $4: 1$ ratio. Preliminary measurements have shown that at the given grain size the reaction proceeds in the kinetic region. Prior to measurement, the catalyst was reduced in the reactor in a nitrogen-hydrogen mixture $\left(3 \% \mathrm{H}_{2}\right)$ at $170-240^{\circ} \mathrm{C}$ and at a flow rate of $3.751 / \mathrm{g} \mathrm{h}$.

Kinetic isotherms (dependence of conversion on the feed rate) were determined at 220, 230, 240 and $250^{\circ} \mathrm{C}$, with feed $0.35-2.3 \mathrm{~mol}$ of the mixture per g and at molar ratios $\mathrm{CH}_{3} \mathrm{OH}: \mathrm{H}_{2} \mathrm{O} 1: 1$, $1: 1 \cdot 1,1: 1 \cdot 3,1: 1 \cdot 5$ and $1: 2$. An example of the course of kinetic isotherms is shown in Fig. 2.

Evaluation of data. The total degree of conversion was calculated from the measured values of the flow rate of the converted gas, from the content of $\mathrm{CO}_{2}$ and of CO , according to the relation

$$
\begin{equation*}
\eta=v\left(\% \mathrm{CO}_{2}+\% \mathrm{CO}\right) / 22 \cdot 4 F n_{0} \tag{3}
\end{equation*}
$$

and the degree of conversion to $\mathrm{CO}_{2}$ according to Eq. (4)

$$
\begin{equation*}
\eta\left(\mathrm{CO}_{2}\right)=v\left(\% \mathrm{CO}_{2}\right) / 22 \cdot 4 F n_{0} \tag{4}
\end{equation*}
$$

where $v$ is the flow rate of the gaseous mixture in $\mathrm{N} / \mathrm{h}, F$ is the total feed of the solution in $\mathrm{mol} / \mathrm{h}, n_{0}$ is the mole fraction of methanol in the solution, $\left(\% \mathrm{CO}_{2}\right)$ and $(\% \mathrm{CO})$ are the contents of the respective components in the gaseous mixture.

The reaction rate can be derived from the dependence of the conversion on the quantity $W / F$, where $W$ is the amount of catalyst in $g$ and $F$ is the feed of the solution in $\mathrm{mol} / \mathrm{h}$, according to the relation

$$
\begin{equation*}
r=n_{0} \mathrm{~d} \eta / \mathrm{d}(W / F) . \tag{5}
\end{equation*}
$$

The determination of reaction rates was carried out both by graphical derivation of the individual kinetic isotherms in the respective points of $\eta_{i}$ and by numerical derivation. In the latter case, the kinetic isotherms or their inversion functions were interpolated by a polynomial of the 2 nd or 3 rd order

$$
\begin{equation*}
W / F=a_{0}+a_{1} \eta+a_{2} \eta^{2}+a_{3} \eta^{3} \tag{6}
\end{equation*}
$$

and the values of derivation of Eq. (6) by $\eta$ were calculated. The reaction rate, as defined by Eq. (5) is then given by the expression

$$
\begin{equation*}
r=n_{0} /\left(a_{1}+2 a_{2} \eta+3 a_{3} \eta^{2}\right) . \tag{7}
\end{equation*}
$$

The values of reaction rates, obtained by the two methods, were compared and evaluated. It turned out that the differences lie within the limits of $5 \%$ maximum which
means that with respect to the experimental errors of the kinetic measurements the agreement is fairly good. Nevertheless, the numerical method of determining the values of reaction rates from the measured kinetic isotherms appears to be more suitable, first of all because it is not charged with errors, arising from the graphical construction of tangents and also because the numerical method can easily be adapted for computing which makes the evaluation easier, especially when a great set of data is available. The values of constants of the respective polynomials (6) for kinetic isotherms, as obtained by the method of least squares, are summarized in Table III.

Determination of the effect of reverse reaction. To ascertain the effect of reverse reaction conversions of methanol were followed in the presence of higher concentrations of the reaction products, i.e. hydrogen and carbon dioxide. The presence of both components was found to have no effect on the reaction course in the measured temperature range and concentration range and thus the effect of reverse reaction is negligible.

## DISCUSSION

The main products of the conversion reaction are carbon dioxide and hydrogen which corresponds to the over-all reaction $(A)$. In all cases the converted gas contains also carbon monoxide. In accordance with the theoretical analysis its content is the lower, the higher is the excess of water vapour and the lower is the conversion temperature. However, the experimentally found content of CO was in most cases lower than that derived by theoretical calculations for the respective degree of methanol conversion, assuming the two-step course of the reaction. The same conclusion was also made

Table IV
Values of Constants of Eq. (8) in Dependence on Temperature and Their Statistical Test

| $t,{ }^{\circ} \mathrm{C}$ | $\left(\mathrm{molCH}_{3} \mathrm{OH}\right) \mathrm{g}^{-1} \mathrm{k}^{-1}$ | $\sigma_{\mathrm{k}} \cdot t_{ \pm}{ }^{a}$ | $m$ | $\sigma_{\mathrm{m}} \cdot t_{ \pm}{ }^{\text {a }}$ | $n$ | $\sigma_{\mathrm{n}} \cdot t_{ \pm}{ }^{\text {a }}$ | $\overline{\Delta r}^{\text {¢ }}{ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 220 | 0.0742 | 0.0003 | 0.49 | 0.020 | 0.48 | 0.024 | $4 \cdot 1$ |
| 230 | $0 \cdot 1418$ | 0.0003 | $0 \cdot 41$ | 0.005 | 0.61 | 0.009 | $3 \cdot 8$ |
| 240 | 0.2308 | 0.0010 | $0 \cdot 41$ | 0.005 | $0 \cdot 60$ | 0.009 | $3 \cdot 0$ |
| 250 | 0.3849 | 0.0035 | 0.36 | 0.004 | 0.74 | 0.006 | $2 \cdot 0$ |
| Aterage |  |  | 0.42 |  | 0.60 |  |  |

${ }^{a} \sigma_{i} \cdot t_{ \pm}$Product of scattering of the respective constant and of the critical value of $t_{ \pm}$for the determination of the reliability interval ${ }^{17}$. ${ }^{b} \overline{\Delta r_{r}}$ Mean relative deviation of the reaction rate.
by Prigent and coworkers ${ }^{5}$. This fact can be explained so that a part of CO is consumed in parallel proceeding reactions, yielding higher alcohols, acetic acid and formaldehyde which were found in small amounts in the condensed product.

The content of carbon monoxide, however, is small in all cases so that the difference between the total conversion and the conversion to carbon dioxide is only small, and consequently also the reaction rate of total conversion of methanol differs only little from that of conversion to carbon dioxide. At the content of $0.6 \% \mathrm{CO}$ the difference in the reaction rates is about $5 \%$, at $1.4 \% \mathrm{CO}$ the error is about $14 \cdot 5 \%$. With respect to the fact that in most cases the content of CO is lower than $0.6 \%$, only total reaction rates of methanol conversion were determined for simplicity sake and these values were used for further deductions and discussions on the reaction course.

In the first step the measured data were correlated with the empirical kinetic equation in the power form

$$
\begin{equation*}
r=k p_{\mathrm{A}}^{\mathrm{m}} p_{\mathrm{B}}^{\mathrm{n}} p_{\mathrm{C}}^{\mathrm{q}} p_{\mathrm{D}}^{\mathrm{s}} \tag{8}
\end{equation*}
$$

( $\mathrm{A}=\mathrm{CH}_{3} \mathrm{OH}, \mathrm{B}=\mathrm{H}_{2} \mathrm{O}, \mathrm{C}=\mathrm{CO}_{2}, \mathrm{D}=\mathrm{H}_{2}$ ).
Since it was experimentally found that the reaction rate does not depend, in the studied region, on partial pressures of carbon dioxide and of hydrogen, the equation can be written in the simplified form

$$
\begin{equation*}
r=k_{1} p_{\mathrm{A}}^{\mathrm{m}} p_{\mathrm{B}}^{\mathrm{n}} \tag{9}
\end{equation*}
$$

The values of constants $k_{1}, m$ and $n$ were obtained by the method of linear regression using the computer Tesla 200. The results are presented in Table IV. From these results it follows that the equation of the reaction rate of conversion can be written in the form

## Table V

Dependence of the Values of Rate Constant $k_{2}$ in Eq. (II) on Temperature and Their Statistical Test

| ${ }^{\circ} \mathrm{C}$ | $k_{3}$ <br> $\left(\mathrm{~mol} \mathrm{CH}_{3} \mathrm{OH}\right) \mathrm{g}^{-1} \mathrm{~h}^{-1} \mathrm{~atm}^{-1}$ | $\sigma_{\mathrm{k}_{3}} \cdot t_{ \pm}$ | $\overline{\Delta r}_{\mathrm{r}}$ <br> $\%$ |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 220 | 0.0760 | 0.00001 | 4.5 |
| 230 | 0.1433 | 0.00002 | 4.3 |
| 240 | 0.2368 | 0.00005 | 3.0 |
| 250 | 0.3591 | 0.00020 | 2.2 |

$$
\begin{equation*}
r=k_{2} p_{\mathrm{A}}^{0.4} p_{\mathrm{B}}^{0.6}, \tag{10}
\end{equation*}
$$

in which the reaction rate is described with an average error of $3 \cdot 1 \%$. When written in the simplified form

$$
\begin{equation*}
r=k_{3}\left(p_{\mathrm{A}} p_{\mathrm{B}}\right)^{0.5} \tag{11}
\end{equation*}
$$

the equation still fits very well the reaction course with an average error $3.5 \%$ which still lies within the limits of experimental errors. The values of the rate constant $k_{3}$ were then calculated for equation (11), using the method of linear regression. Their temperature dependence is shown in Table $V$. The dependence of the logarithm of the rate constant $k_{3}$ on the reciprocal value of temperature, $1 / T$, as shown in Fig. 3, was used to calculate the value of the apparent activation energy, $E=24 \cdot 8 \mathrm{kcalmol}^{-1}$.

The mentioned kinetic equation (11) allows a relatively easy calculation of reaction rates for different reaction conditions, as it is necessary e.g. for the calculation of the quantity of the catalyst for the conversion reactor, however, it does not provide any data for speculations on the possible reaction mechanism. However, the noninteger exponents indicate a complex character of the reaction.

In the second step it was attempted to derive and interpret the kinetic relations on the basis of Langmuir-Hinshelwood assumptions. A general derivation of an equation, including both the adsorption of all components and the sequence of elementary reactions, results in a relation of such complexity that its verification and interpretation becomes practically impossible, for the very reason of the great number


Fig. 3
Dependence of $\ln k_{3}$ on $1 / T$


Fig. 4
Dependence of $k_{8}$ on $1 / T$
of constants. Therefore, only the simplified scheme and the irreversibility of the total reaction were considered in deriving the relations.

Let us now assume that the reaction course can be described by the following scheme

$$
\begin{gather*}
\mathrm{CH}_{3} \mathrm{OH}(\mathrm{~g})+\mathrm{n} \stackrel{K_{1}}{\rightleftarrows} \mathrm{CH}_{3} \mathrm{OHn}  \tag{D}\\
\mathrm{H}_{2} \mathrm{O}(\mathrm{~g})+\mathrm{n} \stackrel{K_{2}}{\rightleftarrows} \mathrm{H}_{2} \mathrm{On}  \tag{E}\\
\mathrm{CH}_{3} \mathrm{OHn} \stackrel{K_{3}}{\rightleftarrows} \mathrm{COn}+2 \mathrm{H}_{2}(\mathrm{~g})  \tag{F}\\
\mathrm{COn}+\mathrm{H}_{2} \mathrm{On} \stackrel{K_{4}}{\rightleftarrows} \mathrm{CO}_{2}(\mathrm{~g})+\mathrm{H}_{2}(\mathrm{~g})+2 \mathrm{n} \tag{G}
\end{gather*}
$$

Kinetic relations are derived, assuming always one single controlling reaction in which the reverse reaction is neglected. The assumptions employed and the respective derived equations are summarized as follows:
a) The controlling step is the adsorption of methanol on one centre:

$$
\begin{equation*}
r=\frac{k_{4} p_{\mathrm{A}}}{1+K_{2} p_{\mathrm{B}}+\left(K_{2} K_{4}\right)^{-1} p_{\mathrm{C}} p_{\mathrm{D}} p_{\mathrm{B}}^{-1}+\left(K_{2} K_{3} K_{4}\right)^{-1} p_{\mathrm{C}} p_{\mathrm{D}}^{3} p_{\mathrm{B}}^{-1}} \tag{12}
\end{equation*}
$$

b) The controlling step is the adsorption of water vapour on one centre:

$$
\begin{equation*}
r=\frac{k_{5} p_{\mathrm{B}}}{1+K_{1} p_{\mathrm{A}}+K_{1} K_{3} p_{\mathrm{A}} p_{\mathrm{D}}^{-2}+\left(K_{1} K_{3} K_{4}\right)^{-1} p_{\mathrm{C}} p_{\mathrm{D}}^{3} p_{\mathrm{A}}^{-1}} \tag{13}
\end{equation*}
$$

c) The controlling step is the surface decomposition of methanol on one centre:

$$
\begin{equation*}
r=\frac{k_{6} K_{1} p_{\mathrm{A}}}{1+K_{1} p_{\mathrm{A}}+K_{2} p_{\mathrm{B}}+\left(K_{2} K_{4}\right)^{-1} p_{\mathrm{C}} p_{\mathrm{D}} p_{\mathrm{B}}^{-1}} \tag{14}
\end{equation*}
$$

d) The controlling step is the surface reaction of carbon monoxide with water vapour on two centres:

$$
\begin{equation*}
r=\frac{k_{7} K_{1} K_{2} K_{3} p_{\mathrm{A}} p_{\mathrm{B}} p_{\mathrm{D}}^{-2}}{\left(1+K_{1} p_{\mathrm{A}}+K_{2} p_{\mathrm{B}}+K_{1} K_{3} p_{\mathrm{A}} p_{\mathrm{D}}^{-2}\right)^{2}} \tag{15}
\end{equation*}
$$

e) The controlling step is the surface conversion of methanol by water vapour on two centres:

$$
\begin{equation*}
r=\frac{k_{8} K_{1} K_{2} p_{\mathrm{A}} p_{\mathrm{B}}}{\left(1+K_{1} p_{\mathrm{A}}+K_{2} p_{\mathrm{B}}\right)^{2}} . \tag{16}
\end{equation*}
$$

The values of the individual constants for the suggested Eqs (12) - (16) were evaluated, similarly as for the power form of the equation, from the experimentally obtained reaction rates using the method of non-linear regression and the validity of the proposed relations was verified.

The found dependence of the reaction rate on concentration of the components in the feed indicates that the reaction rate depends on the partial pressure of methanol approximately in the same way as on the partial pressure of water vapour, which follows also from the power equation (11). However, Eqs (12) - (14) do not conform with this assumption. In numerical evaluation the constants of these equations can even attain negative values and the dependences of reaction rates derived from these equations do not agree with the experimentally found ones. This means that Eqs (12)-(14) do not provide an adequate description of the reaction course and their validity for this case is not satisfactory. Owing to the non-reality of the values of individual constants neither Eq. (15) can be applied to describe the kinetics of the system. An expression formally identical with Eq. (16) is also obtained from Eq. (15) which can be simplified under certain assumptions. The experimentally measured reaction rates in excess hydrogen revealed the independence of the reaction rate of $p_{\mathrm{D}}$. In this case the partial pressure of hydrogen can be taken as constant and relation (15) is, after simplification, identical with Eq. (16), except for constant $K_{1}$ which then represents a combination of the adsorption constant of methanol and of the equilibrium constant of the methanol decomposition. The values of the evaluated constants together with the testing of Eq. (16) are presented in Table VI. From the results found it follows that the form of Eq. (16) expressed the course of the studied reaction under the given experimental conditions with an average error $5 \cdot 8 \%$, as shown in Fig. 4. The value of the apparent activation energy, calculated from the plot $\ln k_{8} v s 1 / T$,

## Table VI

Dependence of the Values of Constants of Eq. (16) on Temperature and Their Statistical Test

| ${ }^{\circ} \mathrm{C}$ | $k_{8}$ <br> $\left(\mathrm{molCH} \mathrm{CH}_{3} \mathrm{OH}\right)$ <br> $\mathrm{g}^{-1} \mathrm{~h}^{-1}$ | $\sigma_{\mathrm{k}_{8} \cdot t_{ \pm}}$ | $K_{1}$ | $\sigma_{\mathrm{k}_{1}} \cdot t_{ \pm}$ | $K_{2}$ | $\sigma_{\mathrm{k}_{2} \cdot t_{ \pm}}$ | $\overline{\Delta r}_{\mathrm{r}}$ <br> $\%$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |
| 220 | 0.332 | 0.013 | 2.33 | 0.52 | 1.51 | 0.31 | 3.6 |
| 230 | 0.577 | 0.014 | 3.35 | 0.34 | 1.37 | 0.15 | 5.8 |
| 240 | 0.716 | 0.016 | 4.63 | 0.59 | 1.30 | 0.17 | 5.9 |
| 250 | 1.277 | 0.084 | 5.61 | 0.72 | 1.25 | 0.13 | 8.5 |

is $E^{\prime}=18.9 \mathrm{kcalmol}^{-1}$. Its numerical value is in this case lower in comparison with the value of the activation energy calculated from the temperature dependence of the rate constant $k_{2}$ from Eq. (11). One explanation is that in Eq. (11) constant $k_{2}$ represents the rate constant of the over-all reaction which includes further tempera-ture-dependent parameters, whereas in Eq. (16) constant $k_{8}$ is merely the rate constant of the rate limiting reaction and the temperature-dependent parameters $K_{1}$ and $K_{2}$ which would also affect the value of the total activation energy appear in Eq. (16) explicitly.

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